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- I.** . . . , , 1989
- II.** . . . , . . . , 1926
- III.** . . . , . . . ,  
1760 . . . , 1984
- IV.** . . . ,  
1760 . . . , 1990
- V.** . . . , . . . , 2005
- VI.** . . . ,  
*Aleae*, 2005  
*Liber de Ludo*
- VII.** . . . , . . . ,  
2001
- VIII.** . . . , . . . ( . . . ), 1869
- IX.** . . . ,  
Delambre (1827), 1829,
- X.** . . . , “ . . . ”.  
. . . , 1837 – 1847 ( . . . ), 2003

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Google, . Oscar Sheynin.

[v]

. 8, 9, 12 13.

Donahue,

(Sheynin 1993, § 2.1).

( , § 3.6), (

, § 4.1)

( 2013,

§ 2.2.4).

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( ). , ,

8, . . .

( . § 3):

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8. !

( , , ),



(1964). , Batten (1988, . 152 – 153)

Friesleben (1971) , 1869 .

5 1833 . 1

(1947, . 360). Morando (1995, . 233)

[ix]

Thoren (1972, . 75) ( 1973, . 109 – 110),

xl

2004 .

(1971), ; Cohen

[x]

1864 . (1861),

Rice & Seneta (2005)

! , (Sheynin 2015, .5) ,

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, 2,5, ,

! ( 1882 . )

1842 . , tg =

sin = cos = 0, sec = cosec

ctg = ±√-1 .

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## 1.

(1667 – 1735)

<sup>1</sup>. 1704 .

, 1712 .

Aitken (1892), Beattie (1935)

(*Dictionary of National Biography*, DNB).

(1657), .

(1692

)  
(1712)<sup>2</sup>.

. Todhunter (1865).

Pearson (1978),

Bartholomew (1984) Stigler (1986).

(Gregory

Collection, MS Dk.1.2. Fol. B [no. 19]).

1694 . (1661 – 1708)

<sup>3</sup>  
. DNB. Ross

(1956)

1694,

1694 .,

, 1694 .,

11 ; 10

1692 ., , a

1712 . [ ]

1690 .

(1690), . Todhunter (1865, . 47).

*Eruditorum*, 1690

Hiscock (1937)

*Acta Eruditorum.*

2.

$\binom{p}{1}$

$$n^p - b^p - C_p^1 b^{p-1} - C_p^2 b^{p-2} + C_p^3 b^{p-3} - \dots, \quad (1)$$

$$b = n - 1. \quad n^p, \quad (i + 1), i = 1, \dots, p,$$

Montmort (1708/1713, XIII, c. 40).

$$= 1, 2, \dots, p, \quad b = n - 3 \quad b^{p-1} \quad 3^i, i$$

1693 .<sup>4</sup>

(1)

(1692). X, XI XII  
X XI

, = 1, 2, ..., 5,

12

, = 1, 2, 4.

XII,-

= 3

= 10





$$1/10^{251,030}$$

$$8/10,000.$$

3.

1712 .

( ) .

$n$

$$C_n^{n/2} \div 2^n .$$

$$n = 2, 4, 6, 8$$

$n$

82

$$1/2^{82} .$$

[ 7 ? ]

1712 .

4

8

1712 .

1. 1712 .

2 3, § 2. , , 1712

1712 .  
1712 .  
[...].

( ),  
22 56.  
22 , 56 .  
3  
47:1.

238  
18. 22 , 34 ,  
[...]

(1693), 1/2  
 $34 \cdot 22$ ,  $34q_{22}$  (  
).  
34 ,  $1/2^7$ , . . .  
1/128, 1/48.  
 $34 \cdot 22$ ;  
 $34 \cdot 22 = 282/586 = 0,482$ ,  $33 \cdot 22 = 292/586 =$

$33 \cdot 22$   
0,498.

1712

22 34 . ,  
34.  
753 - 510 . . . , .  
243 238, .. , Scullard  
(1980, . 420).

111

2024  
18-19  
19

$${}_{19}q_{14} = 1/5 (14 - 33, \dots, 1:4),$$

$$111 \quad 1:(4^{111} - 1). \quad 19$$

( . . ).

9

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66

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33

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$$[ \quad ] \quad 2$$

$$\dots (np + p/2) = 101,$$

101

3669

111

111

2024

(Not:),

(then)

34

3669

111  
, 2024.

(1/48 , , 1/128).

(19q14)

(34 22),

111

33

66

2,

3669 1/2,  
(66·111 + 11 + 1)/2 = 3669  
Shoesmith (1987)

(np + p + 1)/2 =  
(66·111 + 111 + 1)/2 = 3719.  
1712

1692

1693

( Bentley 1976).

1712

Beattie (1935, . 282 – 284 312 – 313). Aitken (1892, . 121 124)

1712 . Stigler (1977),

#### 4. 1712 .

130, 193, 197) (1865, .

$1/2^{82}$ .  
. Shoesmith (1985, 1987).

. 1712 .

Chamberlayne,

(1987): 1711 ., . Ross (1956) Shoesmith

& Lessard 1986; Charnov 1982). (Karlin

5.

(1865, . 48 – 53)  
(1738)

1712 .:

(1)

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1693 .,

*i*

6*i*

, *i* = 1, 2, 3. David (1962, .

126 – 129)

1756 .,

1717 .,

1714 .,

(1714, 1738).

S. M. Stigler

L.

D. A. Sprott  
Lefkovitch

6.

[...]

1694 .

1696 .,

1694 . ,

1694 . ,

1705- , 1708-

1694 . Ross

(1956),

(1969) , 1698

1703 . 1703 .

XVIII .

1698 .

(1956, .950)

2024 . [

1694- ( !).

1694- .]

1. -

2. (1961)

(1865, .619),

, 1710.

1710 .

3. Saville Professor. *Phil. Trans.* 1710- 1712 . Henry

Saville ( . , ) .

4.

5. 1818 .

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6. . . . .
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8. . 7.
9. Samuel Pepys, . . . . ., 1633 – 1703,

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(1924; 1925)<sup>1</sup> ( ) ,

*Approximatio* 12 1733 . *Approximatio*

. *Approximatio*

(1730). . . :

10! 900!

$\frac{14-}{10!}$

1733 .

12

1730 .

(1865),

(1738; 1756),

. 184, 192 193

(1756, . 243 – 250).

<sup>23</sup>  
(1865, §§ 324 325)

1756 ., 1865 ., ? ( ,  
[ ] ):  
12

1733 .

, ,  
 , 1738 . *Approximatio*  
 [ ] *Isis.*  
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*Approximatio.*  
 , 1730 .,  
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*Approximatio* , , ,  
 , 1733 .  
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 1738  
 10 50,  
 1756 . 160 .[...] ,  
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 ,  
*Approximatio* , ,  
 6 1/2  
 11 1/2 18 . 8 1738 .  
 . § 335

*Approximatio,*

XVIII .

*Nature*

[ 1738 1756 .]

[1733 .]

1756 .

*Isis.*

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[...], , , , ,  
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<sup>1</sup>. 1757 .

(Simpson 1756, 1757; Seal 1949; Plackett 1958; Sheynin 1973 ).

: 1757 .

. 1760 .

(Eisenhart

1961; Sheynin 1973b, 1977; Stigler 1973).

[ , !]

1710 .

Clarke (1929),

1761 .

Wallis (1981).

( , ),

[ , ], 1711 .

1760 .

(Hill 1961; Markovic 1981)

[ !]

], ( - ).  
(1929).

Boscowitz).

[...]  
1760-  
1760  
1744 .. 16

**2.**

XVIII .

**Boscowitz**

*a, b, c, d, e, ...*

- 1.
- 2.
- 3.

*p, q, r, s, t.*



$$a + p, b + q, c + r, d + s, e + t.$$

$$1. a + p - b - q, b + q - c - r, c + r - d - s, d + s - e - t.$$

$k, l, m,$

$n.$

$$2. p + q + r + s + t = 0.$$

3.

$$\begin{array}{l} \dots \\ + w, \dots, \end{array} \quad \begin{array}{l} x, x + y, x + z, x + u, x + w, \dots \\ a + x, b + x + y, c + x + z, d + x + u, \\ \dots, \dots, \dots, \dots, \dots \\ p, q, r, s, \dots \end{array}$$

$$+ z = \frac{p(+y)}{q}, \quad + u = \frac{p(+y)}{r}, \quad + w = \frac{p(+y)}{s}, \dots$$

$$z = \frac{p}{q} - \frac{py}{q}, \quad u = \frac{p}{r} - \frac{py}{r}, \dots$$

$$x, x + \frac{p}{q} - \frac{py}{q}, x + \frac{p}{r} - \frac{py}{r}, \dots$$

:

$$nx = + + \dots, -\frac{p}{q} - \frac{p}{r} - \frac{p}{s}, \dots, -py[\frac{1}{q} + \frac{1}{r} + \frac{1}{s}], \dots$$

$$x = k + Uy \quad A + A_1y,$$

$$B + B_1y, C + C_1y, \dots (A, A_1, B, B_1, \dots)$$

$$A + A_1y, B + B_1y, \dots, \dots$$

$$y = A/A_1, B/B_1, \dots$$

$y,$

$$(X_1, Y_1), (X_2, Y_2), \dots,$$

$$\hat{Y}_1 = 0 + {}_1X_b$$



$$\hat{Y}_1 = a + x, \hat{Y}_2 = b + x + y, \dots$$

$$\begin{aligned} + y &= \hat{Y}_2 - \hat{Y}_1, & &= Y_2 - Y_1, \\ + z &= \hat{Y}_3 - \hat{Y}_1, & &= Y_3 - Y_1, \dots \end{aligned}$$

$p, q, r, s$

$$p = 1/(X_2 - X_1), q = 1/(X_3 - X_1), r = 1/(X_4 - X_1), s = 1/(X_5 - X_1).$$

$$\begin{aligned} + z &= p(\quad + y)/q, \dots & & \hat{Y}_i - \hat{Y}_1, \\ \hat{Y}_2 - \hat{Y}_1, & & & z, u, \dots & z \\ R_3 - R_1 &= \end{aligned}$$

$$\frac{X_3 - X_1}{X_2 - X_1}(Y_2 - Y_1) - (Y_3 - Y_1) + \frac{X_3 - X_1}{X_2 - X_1}(R_2 - R_1).$$

$$x = R_1,$$

$$\frac{x + y}{n} R_1 + (R_2 - R_1), \quad R_i,$$

$$( \quad ) - y = -py/p,$$

$$nR_1 =$$

$$\sum_{i=3}^n (Y_i - Y_1) - \sum_{i=3}^n \frac{Y_2 - Y_1}{X_2 - X_1} (X_i - X_1) - \frac{R_2 - R_1}{X_2 - X_1} \sum_{i=3}^n (X_i - X_1).$$

$$\begin{aligned} R_1 &= k + U(R_2 - R_1), & k &= U \\ X_i &= Y_i. & R_1 & \end{aligned}$$

$$y = R_2 - R_1:$$

$$R_1 = A + A_1(R_2 - R_1), A = k, A_1 = U,$$

$$R_2 = B + B_1(R_2 - R_1), R_3 = C + C_1(R_2 - R_1), \dots$$

$A, B, C$

$X_i, Y_i.$

$$\begin{aligned} R_i &= 0, & n & & y = R_2 - R_1, & - \\ A/A_1, -B/B_1, -C/C_1; & & & & & \\ & & & & R_i & \\ & & & & * & \end{aligned}$$

$$R_1 = A + A_1 y^*, R_2 = B + B_1 y^*, \dots \quad (2)$$

$$R_i = 0 \quad (2) \quad R_i$$

$$R_i = \bar{Y} - Y_i - (\bar{X} - X_i) \left[ \frac{Y_2 - Y_1}{X_2 - X_1} + \frac{R_2 - R_1}{X_2 - X_1} \right] =$$

$$\bar{Y} - Y_i - (\bar{X} - X_i) \frac{\hat{Y}_2 - \hat{Y}_1}{X_2 - X_1} = \bar{Y} - Y_i - \frac{\bar{X} - X_i}{1} =$$

$$\bar{Y} - Y_i - \frac{\bar{X} - X_i}{1}$$

$R_i$

0,

1,

$b_i =$

$$\frac{\bar{Y} - Y_i}{\bar{X} - X_i}$$

27

$b_i$

$n$

(Eisenhart 1961; Stigler 1973; Sheynin 1977).

### 3.

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- Clarke (1929);
- (1755), 8 1754 . 13
- 1756 . . .
1. ( ),
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  3. ( ) . Monjardet (1991).
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1760 .

R. W. Farebrother, Further details of contacts between Boscovich and Simpson in June 1760. *Biometrika*, vol 77, 1990, pp. 397 – 400

1.

Stigler [iii]

, .

1.  $b,$

$n$   
( $a, b$ )

$n = 4:$

$(x_i, y_i), i = 1, 2, \dots, n,$

$$\sum_{i=1}^n [(x_i - a)^2 + (y_i - b)^2] = \min. \quad (1)$$

2.  $b,$

$n$

$(x_i, y_i), i = 1, 2, \dots, n, \quad y = a + bx$

$$\sum_{i=1}^n (y_i - a - bx_i) = \min \quad (2)$$

$$\sum_{i=1}^n (y_i - a - bx_i) = 0. \quad (3)$$

*Boscovitz* ([ ], . 616)

– 1760 .

, (. 619) ,

1989 .

(Paoli 1988),

( . 127), 12

1760 .

( ),

( . 131), 27

1760 .,

**2.**

C. E. J. Griffiths

27

1760 . [

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[...].

, *Bevis*,

[ ] ,

*Stay*,

[

?] ,

[...].

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[...]

[...]

([iii], . 616 – 617),

**3.**

§ 2

12 26

1760 .

[

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1764 .,



182)<sup>1</sup>. (Paoli 1988, .  
(. 127, 145)

(Glaisher 1873, . 112; XVIII .  
([iii], . 618)

(1760)

(1986; Farebrother 1990).

([iii], . 619),  
(1988, . 127): 12 1760 .

(. 131),  
[1709 – 1784,  
1755 1883] . Boswell (1791,  
. 181, 272)

#### 4.

([iii], . 619),  
. § 5.

(Tannery & Henry 1891, . 513)

De La Chambre (Tannery & Henry 1894, . 358),

[B] DB[F].

#### 5.

(1)

$$\sum_{i=1}^n w_i \sqrt{(x_i - a)^2 + (y_i - b)^2}, \quad (4)$$

$w_1, w_2, \dots, w_n$  - Kuhn (1967, . 39 – 40)

(1750)  $n = 3$  (1638/1891, . 153), . ,  
 $n = 3$   $w_1 = w_2 = w_3 = 1$ . ( 1754 – 1756  
 .)  $n = 4$

$n = 3$   
 ,  
 ,  
 ,  
 $n$ .

Boyer (1959, . 205 – 206)  
 De La Chambre 1657 .  
 Clerselier 1662 . (Tannery & Henry 1894, . 354 – 358  
 464 – 484),

( . § 4),  
 $b$  (4)  
 $n = 2, a = 0$   $w_1 = 2w_2$   $w_2 = 2w_1$ .  
 ,  $x_1 = x_2 = \dots = x_n$   $a = x_1$  (4)

$w_i y_i - b$ .

$y_i$   
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 618)  $w_i = \bar{X} - X_i$   $y_i = (\bar{Y} - Y_i) / (\bar{X} - X_i)$ .  
 , , Kuhn (1967)

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(Field 1988).

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(Settle 2003).

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(Thoren 1990):

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*Science*, .84, 1936, .289 –

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14. A. E. L. Davis,
15. , . 58, . . .
16. . Davis (1981). . 35
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# VI

## *Liber de Ludo Aleae*

David Bellhouse, Decoding Cardano's *Liber de Ludo Aleae*.  
*Hist. Math.*, vol. 32, 2005, pp. 180 – 202

### 1.

(1657)  
(1953, 1966), XVI . ( :  
LLA), 1650-  
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1564 . , , ;  
1663 . (Cardano 1966). ,  
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XVII . , XVIII . ,  
Cotton (1674),  
Hoyle (1743).  
, LLA  
1953) LLA (Cardano  
, De Mora Charles (1981)



Franklin (2001),  
 LLA  
 Ore (1953).  
 Jensen (1994),  
*De Subilitate* [ , 1550]  
*De Rerum Varietate* [ , 1557].  
 Margolin (1976),  
 LLA  
 Tamborini (1999)  
*fortuna* LLA  
 LLA  
 LLA  
 1654  
*Vetula*, 1250<sup>2</sup>. *De*  
 2. (1501 – 1576)  
 LLA  
 Fierz (1983), Ore (1953) Rose (1975),  
 Cardano (1930).  
 XVI  
 XIX  
 [?]

(Grendler 2002, . 408 – 409; Grafton 1999, . 42).  
LLA

XIII XVI

(Lieber 1968;  
Mack 2002).

(Grendler 1989) ,  
. Van Egmond (1981)

*Liber Abaci*

1600 .  
(Fibonacci 2002).

. Uqlidisi (1978).

(Van Egmond 1981).

(Peterson 1997).

Van Egmond (1981),  
1477 .  
1600 ., , 55 %  
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(Kline 1972; Masi  
1983; Schrader 1967). XII XIII

Rose (1975).

(Laird 1991),

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(Grendler 2002).

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Egmond (1981),

Smith (1970)

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Maclean (1994)

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, *De Ludis*.

1525 . Ore (1953)

, David (1962)

*De Subtilitate*

1551 .

*De Ludis,*  
*Practica Arithmetice.*

. Tamborini (1999)

(Cardano 1966),

Naudé, 1643 (Cardano 1930). Jean Stoner (Cardano 1930, . xiii),

Naudé:

*Gabriel Naudé*

5, . *Naudé*

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(Cardano 1968). Feldmann (1961)

Siraisi (1997)

; . Grafton (1999)

(Kessler 1994).

**3. *Liber de Ludo Aleae***

Ore (1953), LLA

Todhunter (1965),

LLA

Cardano (1930)

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1274) (1225 –  
(Thomas Aquinas 1975, *Summa Theologiae* 2 2 .32,7).  
(1972; *Summa Theologiae*  
2 2 .118,8), .4, i, 43,  
Aristotle (1955):  
(1991),  
*De Remediis* . I, 26 27; . II, 16)  
(1971, . 222 –  
223)  
*Platina,*

(Platina 1998, . 109).

(Castiglione 1967, . 140). [

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(1953, . 6)

LLA.

( utilitas, . . . ).

(2000, . II, 10 20),

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LLA,

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*in utramque partem,*

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Franklin (2001)<sup>6</sup>

*utramque partem.*

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(1955, . 177 – 178). ( . V, iii, 5 – 6)

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*circuit*, (1953, . 18)

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Sambursky (1956), Sheynin (1974), Hacking (1975)<sup>7</sup> Styan (1998).

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; Ore (1953, . 161)

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Broome (1984)

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(1955, § 3).  
LLA, [ ] [ ] (Lucrum enim a volentibus, atque scientibus optimum est).

*volentia*,  
*scientia*

*in utramque partem.*

(§ 3),

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Gambling *Catholic Enc.* (Herbermann 1907).

*scientia* ( , ). – LLA.

*volentia*, *scientia* ,

*scientia*

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§ 3.

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(scientia),  
[...]  
XVI  
(1993).  
scientia  
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*De Subtilitate*, . 18.  
. Maxwell-Stuart (1998).  
Grafton (1999).  
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(1967) : , . IV

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### 6. *Liber de Ludo Aleae*

1995). , (Nauert

, Celenza (1999, . 48) :

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David (1962), LLA

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Calcagnini (1544, . 286 – 300), *De talorum ac tesserarum et  
calcolorum.* , [...], tessera –  
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Calcagnini.  
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. Hagstroem (1932),

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*De Remediis*, . I, 26 (Petrarca 1991, . 1,

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 [Petrarca (1991, . 1, . 83)  
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**7. De Vetula**

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*De Vetula* ( ), 20  
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*De Vetula* . . . cadentia,

(David 1962).

*De Vetula,*

*Vetula.*

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*De Vetula*

. Krischer (1994)

. Kendall (1956)

*De Vetula*

*Vetula,*

*De*

(Anonymous 1475?; 1479).

*De Vetula*

(further),

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*De Vetula*

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*De Vetula*

(Robathan 1968).

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*De Vetula*

[ ]. [ ] ,

(1978). XVI . , Thalmann

Gataker (1619)

(Chaucer 1977, . 227):

1/6, : 5 3. 7

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, 1492 – 1556, , . 480 – 524,

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**Cardano G.**

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Jeff Loveland, Buffon, the certainty of sunrise  
and the probabilistic reductio ad absurdum.  
*Arch. Hist. Ex. Sci.*, vol. 55, 2001, pp. 465 – 477

1777 .

XIX XX  $2^n$   $2^{n-1}:1$ .

1, XVIII .

1764)<sup>2</sup>

(1774; 1814/1994, . 11)

$(n + 1)/1$ .

(Todhunter 1865, . 344)

(Pearson 1978, . 193 – 194 660)<sup>4</sup>.

Zabell (1988, . 175 – 177)

. 368),

1764 ..

1750-  
(1777, § 6),

( 1764/1970, . 150 – 151):

?

10, 20, 100

5

(réduire)

2 190

1, 2, 4, [...]  
n = 2 190 000,

$$2^{n-1} = 2^{2\,189\,999}$$

o

3:1.

000,

( § 8).

1/10

6

$2^n:1$

2.

XVIII . 1750-

1.

(1690, . 1, . 184),

William Molyneux,

( , . 186 – 188).



1740- – 1750-

2.

(1777)

Cicero (45 – 44 . ., . 2, 15 – 17, . 52 – 53).

. Holcot (1331 – 1334, . 151) Rivo  
(Fernand de Cordova 1470, . 101, 125), . Rivo (1465, . 39;  
1470, . 420), – (?)  
Aureolus (1312 – 1320, . 1, . 673), –

D Alembert (1757, . 404 – 405)

XIX .

XVII .

395)

. Lubières (1765, .

(1744 – 1745, 478, . 278 – 279),

Candaux (1993).  
(1744 – 1745, 460, . 265),

Lubières (1765, . 394) ( , 540, . 320).

XVII – XVIII

(human conditions)

91, Brunschvicg)<sup>10</sup> (1670, . 400 – 401,

Leibniz (1714, . 707)

sGravesande (1724, . xl, liii), Buffier (1724, . 307) Hume  
(1739, . 124)

sGravesande (1724)

( . liii) :

[...] , ,

293), (1754, . 292 –

[...] <sup>11</sup>.

1930 .

(1749 ),

3.

$$(2^{n+1} - 1)/1,$$

$n$

$$(2^n - 1)/1,$$

(1777)

$$2^n/1 \quad 2^{n+1} - 1/1$$

$$(x^y - 1)/1$$

$$x^y/1,$$

2.

$$(2^{n+1} - 1)/1$$

$\setminus n$

( )

$$P(x > \frac{1}{2}) = \int_{1/2}^1 x^n dx \div \int_0^1 x^n dx = 1 - (1/2)^{n+1} = \frac{2^{n+1} - 1}{2^{n+1}}.$$

$$(2^n - 1)/1$$

n. Zabell (1988, . 176 – 177)  $2^{n-1}/1$  ,

$(2^n - 1)/1,$

2,

· ,

· ,  $12^{(1777)}$

1, 2, 4, ..., 64, ...  $2^{n-1}.$

$2^n/1,$

$2^{n-1}/1.$

$n$

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$2^n/1$

$2^{n-1}/1?$

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(1749b),

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(1734),

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[ 2013, § 3.2.3],

(1734),

Lignac (1751, . 1, ltr. 2, . 40)

$$(1/2)^6 = 1/64.$$



1/

$$\frac{n}{1/n}$$

(Bru 1988b, . 75 – 76).

. Cicero (45 – 44 / ,

. 2, 15 – 17, . 52 – 53)

XVII .

XVIII .

Arbuthnot (1712)

82

[ ]

$$1/2^{82}, . . .$$

1986, . 225 – 226)<sup>14</sup>.

(Stigler  
s Gravesande (1774)

XVIII .

(Bru

1988 , . 223 – 225)<sup>15</sup>.

, Mairan

(1746, . 60 – 63),

$$. [...] 10^{80}/1.$$

Maupertuis (1752, . 307 – 310)

(Arbuthnot, s Gravesande),  
( ).

[ ]  $1/n$ ,

64/1

(1749b, . 134) :  
64/1

!

1/  $n$

$(n - 1)/1$ .

$2^n/1$

$2^{n-1}/1,$

$n$   
(1777).

Jean Filleau de la Chaise (Anonymous 1672, . 148)

1666 .:

20 !

;

[...]

100,

1000

16

1, 2, 100, 1000, ,

$n$ ,  $1 - 1/n$ .

1/

17  $1/2$ ,  $n$

18

[counterpoint, ?]

(Roger 1989, . 560 – 561).

4.

1778 ., (Stigler 1986, .  
(1754) 103 .; Bru 1988b, . 77).

1749 ., 1750-

XVII . [ ?]

XVIII .

(wholesale)

(Zabell 1997, . 368).

XVIII .

(Bru 1988b, . 73),  
1777 .

XVIII .,

1777 .,  
1764 .

1730- 1740- (Milliken 1965, . 180 –  
181 .).  
1760 .

1848, . 54 .; Hanks 1966, . 42 .). (Gouraud

1762 . (§ 8),

Charles Panckoucke 1765 . (Watts 1969, .

103 – 104).

56

24

[ 1763 . ] .

56 .

1740-

(1749 )

(Sloan 1987, . 132 – 133)

1740- 1750-

1730-

1740-

1760-

1770-

1760-

, 1749 .

1740-

1749 .

(Buffon 1749 , . 62; Sloan 1992, . 213 – 216)

1749 .

(1749b)

Jean-Daniel Candaux,  
Cramer (1744 – 1745)

1. (1950/1964, . 130),
- 2.
- 3.
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6. )
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- 8.
9. ( . 12, . 201 – 204).  
1841 .
- 10.
11. ( . 5, . )).
- 12.
- 13.
14. Shoemith (1985;  
1987) David & Edwards (2001, c. 9 – 11), Freudenthal (1961, c. xi)
- 15.
16. 1672 .,
17. ( . )).
18. ( . 2013, § 6.2).

, 1720 – 1793,  
, 1715 – 1780,  
, 1704 – 1752,

- , 1632 – 1704, , ,
- , 1723 – 1791, , ,
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[?] ,

1851 .  
1837 – 1843 . 8

(Terminbeobachtungen) 1837 – 1841 . ,

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16 1838 .

. 266 – 272. [

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1827 .

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(1920, . 197),

1828 .

*das Gewicht haben, was Ihnen von Rechtswegen gebührt.*

**. 281 – 282.**

[ ] . [...]

15 [1835 .]

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.300 – 305.

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, 1852, . 2, .339).

1833 .

*ordentlich*

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8 1839 .

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1834 – 1836 .

28 1838 .

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.29 1840 .

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. 1846 .

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.1 :

Weisse (1846).

(49 ).

[ *Astron. Nachr.* ]

1853 .

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19

1. Kendall  
& Doig (1968) 10 1830 – 1874  
(1865 ),

(1865b; 1865 ).  
( 1866).

2. (1809, § 175). 1809 1823 . ( )

( 1831).

3. . Zoch (1935)

4. (1912/1999, § 135, . 160),  
1809 .

5. 1839 . (Werke, . 8, . 146  
– 147), ( )

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6. ,

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(1838, § 11)

( 1838)

7. , . . . . .  
 ( . . . . .2)  
 10 : ( . . . . . )  
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8. , (May 1972, . 306).  
 9. XIX .
10. ( , ) . . . . .  
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11. ( ) . . . . .  
 , . . . . .
- (Repsold 1920, . 190 – 191).
12. , . . . . .  
 ( 2016, § 2). , . . . . .  
 14 8 . 1826 . . . . .  
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 ( 2 1817 .), . . . . .  
 , 27 . 1846 - . . . . .  
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 ( . . . . . ) . . . . .  
 - ( . . . . . ) . . . . .  
 ), , (1846), (Bruhns 1875), . . . . .
13. ? ?
14. , . . . . . (1912/1999, . 15), . . . . .  
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15. 1762 ., ordentlich . . . . .  
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16. . . . . .  
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- 1835 . (Freiesleben 1971).
17. , . . . . .  
 .. (1826). . . . .
18. 1846 . . . . .  
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19. ( . 13) . . . . . XIX . . . . .  
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 (Lueder 1812, . 9). Descartes (1637/2012, . 63) , . . . . .  
 ( ?) . . . . .

(Hill & Elkin 1884, . 191).

- , 1799 – 1875,  
 , 1747 – 1826,  
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 , 1788 – 1864,  
 , 1779 – 1854,  
 ( – ),  
 , 1819 – 1905,  
 . 1895 .
- . . (1838, .),  
 . . . . ., 1961, . 226 – 258.  
 . . (1947),  
 . . (1809, .), . 2, . 3.  
 (1957, . 89 – 109).  
 --- (1823, .), . . . . ., . 17 – 57.  
 --- (1826, .), . . . . .,  
 135 – 140.  
 --- (1828, .), . . . . ., . 59 – 88.  
 --- (1957), . . . . ., . 1. .  
 . . (1964), . . . . .  
 . (1912, .), . . . . ., 1999.  
 . . . . . 1905 .  
 . . (1847, .), . . . . ., 1953.  
 . (1866), . . . . .
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# IX

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## Delambre (1827)

F. W. Bessel, J. B. J. Delambre, *Histoire de l'Astronomie  
du dix-huitième siècle*. Paris. 1827.  
*Jahrbucher f. Wiss. Kritik*, Bd. 2, 1829, pp. 161 – 168, 179 – 200

[1]

1.

Montucla [1758; 1799 – 1802]

(1788).

XVIII

wachsenden Verschiedenheit des äußeren derselben sein mag. bei der

XVIII

[2]

(1817; 1819; 1821),

XVIII .,

2.

, J. P. von Wurzelbaur;  
 (1671 – 1732), A. G. Graham (1675 – 1751), J. Sisson,  
 ; – : Macaldis,  
 [ : , -  
 ] J.-B.-C. Bochart de Saron; –  
 Louville (1671 – 1732), (1704 – 1760), ,  
 , ; – , .  
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 , . ; – (1711  
 – 1796), A. P. D. du Sejour, , Ch. Massier  
 (Messier, 1730 – 1817), .

XVIII ..

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 [ 1822 ]. ,

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Taselen

(?), , ?  
 XVIII ,  
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Triduum<sup>6</sup>,

*La Hire* *Römer s*

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[ ], 0,3263, ,5,2.

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[1822 – 1824]

[ 1769 ]

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(Kreise)



XVIII .

[XIX ]

11 .

12 .

228):

[ ] .

[6] Graham, Sisson Bird,

75

*Hist. Astron. Moderne.*

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Louville

*Messier,*

Messier

Marinoni,

[7]

*d'Uranibourg* [Paris, 1680].

*Voyage*

[ ,]

*Si quis vero nonnullas inter observata sua dissensiones pro novis in coelo inaequalitatibus gestiat propalare, eum, nisi simul causis hisce physicis consentaneas ostenderit, Detectoris nomen infeliciter ambire, puta, Astronomiaeque perturbatorem potius quam promoterem, agere.*

mit Maßregeln, welche ein vielleicht nie übertroffenes Beispiel vollendeter Experimentierkunst geben,

( . 628):

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Gael Morris Charles Mason,

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0,1426

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!

die von ihm selbst in jener früheren, nicht die Vorarbeiten der gegenwärtigen besitzenden Zeit, gemachten Untersuchungen, noch in einer späteren,

[10]

[ ]

(Walter).

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397

[La Caille 1847],

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[ ?]



),

(subtraktive?)

21.

4:1.

[11]

22.

23.

(1801),

[!]

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[!] [!]

(Méchain & Delambre 1806 – 1810)

1.

( ), (1796/1982, . 328)

1813 .,

2.

(Delambre 1912).

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(1864),

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(1846, . 385)



(1847, . 182 – 183)  
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 - 1, 1, 0, 1.  
 ), ( (1846, . 393;  
 1847, . 183) (testimony)  
 q:

$$q = 2^{-1}, \quad = 1/2(q + 1).$$

$$0 \quad 1, -1 \quad q \quad 1. \quad , \quad > 1/2,$$

(authority)

$$= -1/5. \quad 2/3,$$

$$3/5 \quad 4/5$$

$$= 1/2), \quad 50% ( \dots )$$

(1846, . 393)

( , . 398).

[...]

[...]



Donkin (1851)<sup>10</sup>,  
(Venn 1962, . ix, 119  
122 – 123).

[ , ]

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) =

(1837b)

[ § 110).

(1837), (1812/1886, .261), (1837,

2g

$$P = \frac{1}{\mu!} [ \mu - \mu(-1)^\mu + C_\mu^2(-2)^\mu - C_\mu^3(-3)^\mu + \dots$$

$$- \mu + \mu(-1)^\mu - C_\mu^2(-2)^\mu + C_\mu^3(-3)^\mu - \dots ]$$

$$2g \quad 2g \quad \mu$$

μ,

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[ ].

1846 .. , 10,  
 - 1930 .<sup>15</sup>, (1837 , .412)

[ = 1/400 , ], . . . , 91,4187

$$\frac{1}{10!} \left[ \frac{92}{100} \right]^{10} \approx 0,00000012.$$

412) ( 1837 , .  
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. 1). ( 1838,

1838, . 27):

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$$1/2^{11} = 1/2048.$$

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(1838, . 27) 10<sup>7</sup>:1.

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$$\frac{1}{2048} \cdot \frac{1}{10!} \left[ \frac{92}{100} \right]^{10} \approx 0,000000000058,$$

20 000 000 000:1.

(. 27 – 28).

(. 28),

*ceteris manentibus*

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(1838, . 26):

100 000 000/100 000 001

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1/100 000 001

( ) = 0<sup>17</sup>.

( / ) = 1.

20 000 000 000:1, . . .

( / ) = 0.

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= ( / )<sup>18</sup>. Hailperin (1986, . 355 – 359)

**6.**

(1847)

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[...]

Mansel T. S. Baynes.

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Stigler (1986, . 157).

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 $a^2 + b^2 = c^2$ , , , ,
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